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Theoretical Fundamentals of Electrical Engineering

Steady states in electrical circuits

Transients in electrical circuits

Electrostatic field. Magnetic field of DC

Alternating field in stationary mediums

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